

Reg. No. : 

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**Question Paper Code : 51315**

B.E./B.Tech. DEGREE EXAMINATIONS, APRIL/MAY 2024.

First Semester

Civil Engineering

MA 3151 – MATRICES AND CALCULUS

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(Common to : All Branches (Except B.E. Marine Engineering))

(Also Common to PTMA 3151-Matrices and calculus for B.E. (Part-Time)  
First Semester-All Branches-Regulations 2023)

(Regulations 2021)

Time : Three hours

Maximum : 100 marks

Answer ALL questions.

PART A — (10 × 2 = 20 marks)

1. If  $\lambda$  is an eigenvalue of a matrix  $A$ , then prove that  $\lambda^2$  is an eigenvalue of  $A^2$ .
2. If  $x = [-1, 0, 1]^T$  is the eigenvector of the matrix  $A = \begin{bmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1 \end{bmatrix}$ , then find the corresponding eigen value.
3. Sketch the graph of the function  $f(x) = 2.0 - 0.4x$  and find the domain of the function.
4. Differentiate  $y = x \tan(\sqrt{x})$  with respect to  $x$ .
5. Verify Euler's theorem for the function  $u = x^2 + y^2 + 2xy$ .
6. If  $u = x - y$ ,  $v = y - z$ ,  $w = z - x$ , then find the Jacobian  $\frac{\partial(u, v, w)}{\partial(x, y, z)}$ .
7. What is wrong with the equation  $\int_{-2}^1 \left[ \frac{1}{x^4} \right] dx = \int_{-2}^1 [x^{-4}] dx = \left[ \frac{x^{-3}}{-3} \right]_{-2}^1 = -\frac{3}{8}$ .
8. Evaluate  $\int_{-1}^1 \left[ \frac{\tan x}{1 + x^2 + x^4} \right] dx$  by using the concept of odd and even functions.

9. Evaluate  $\int_1^2 \int_0^{x^2} [x] dy dx$ .
10. Write the integral equation for the regions  $x \geq 0, y \geq 0, z \geq 0, x^2 + y^2 + z^2 \leq 1$  by triple integration.

## PART B — (5 × 16 = 80 marks)

11. (a) (i) Find the eigenvalues and eigenvectors of the given matrix
- $$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 3 & -1 \\ 0 & -1 & 3 \end{bmatrix}. \quad (8)$$

- (ii) Using Cayley-Hamilton theorem, find the inverse of the given matrix  $A = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 1 & 1 \\ 1 & 0 & -2 \end{bmatrix}$ . (8)

Or

- (b) Reduce the quadratic form  $3x_1^2 + 5x_2^2 + 3x_3^2 - 2x_2x_3 + 2x_3x_1 - 2x_1x_2$  to a canonical form by orthogonal reduction. (16)

12. (a) (i) Find the value of  $\lim_{x \rightarrow 2} \left[ \frac{x^2 - 2}{x^3 - 3x + 5} \right]^2$ . (6)

- (ii) Find the local maximum and minimum values of the function  $f(x) = x + 2\sin x$  in the interval  $0 \leq x \leq 2\pi$ . (10)

Or

- (b) (i) Find an equation of the tangent line to the curve  $y = \frac{e^x}{(1+x^2)}$  at the point  $(1, e/2)$ . (8)

- (ii) Find the absolute maximum and absolute minimum values of the function  $f(x) = \log[x^2 + x + 1]$  in the interval  $[-1, 1]$ . (8)

13. (a) (i) If  $u = \log[x^2 + y^2 + z^2]$  then find the value of  $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2}$ ? (8)

(ii) The temperature at any point  $(x, y, z)$  in space is given by  $T = 400xyz^2$ . Find the maximum temperature on the surface of the unit sphere  $x^2 + y^2 + z^2 = 1$ . (8)

Or

(b) (i) Expand  $f(x, y) = e^{x+y}$  about the point  $(0, 0)$  in powers of  $x$  and  $y$  upto third degree terms by using Taylor's series. (8)

(ii) Find the maxima and minima for the given function  $f(x, y) = x^3y^2[1 - x - y]$ . (8)

14. (a) (i) Evaluate  $\int x^2 e^x dx$  by using integration by parts. (8)

(ii) Evaluate the integral  $\int \sin^4 x dx$ . (8)

Or

(b) (i) Evaluate  $\int \sqrt{a^2 - x^2} dx$ . (8)

(ii) Evaluate  $\int \frac{1}{(x^2 - a^2)} dx$  by using partial fraction. (8)

15. (a) (i) Evaluate  $\int_0^{\pi/2} \int_0^{\sin \theta} [r] d\theta dr$ . (8)

(ii) Change the order of integration in

$\int_0^a \int_x^a [x^2 + y^2] dy dx$  and hence evaluate it. (8)

Or

(b) (i) Evaluate  $\iint [xy] dx dy$  over the positive quadrant of the circle  $x^2 + y^2 = a^2$ . (8)

(ii) Find the volume of the sphere  $x^2 + y^2 + z^2 = 3^2$  by using triple integration. (8)